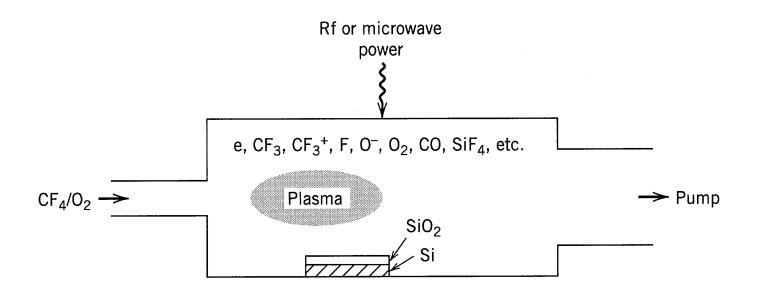
A MINI-COURSE ON THE

PRINCIPLES OF PLASMA DISCHARGES

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OUTLINE

- Introduction to Plasma Discharges and Processing
- Summary of Plasma Fundamentals
 - Break —
- Summary of Discharge Fundamentals
- Analysis of Discharge Equilibrium
- Inductive RF Discharges

ORIGIN OF MINI-COURSE

45 hr graduate course at Berkeley \Longrightarrow

12 hr short course in industry \Longrightarrow

4 hr mini-course

INTRODUCTION TO PLASMA DISCHARGES AND PROCESSING

PLASMAS AND DISCHARGES

• Plasmas:

A collection of freely moving charged particles which is, on the average, electrically neutral

• Discharges:

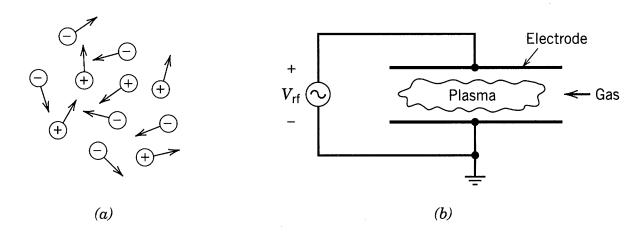
Are driven by voltage or current sources

Charged particle collisions with neutral particles are important

There are boundaries at which surface losses are important

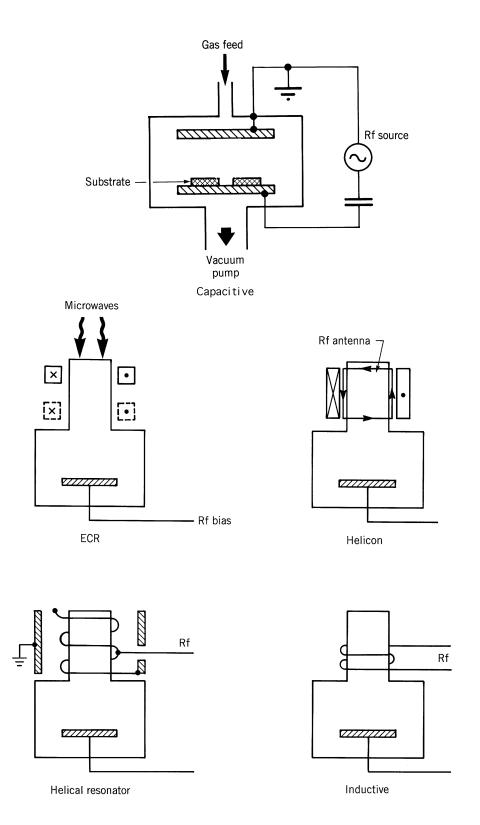
Ionization of neutrals sustains the plasma in the steady state

The electrons are not in thermal equilibrium with the ions



- Device sizes $\sim 30 \text{ cm} 1 \text{ m}$
- Driving frequencies from DC to rf (13.56 MHz) to microwaves (2.45 GHz)

TYPICAL PROCESSING DISCHARGES



RANGE OF MICROELECTRONICS APPLICATIONS

• Etching

Si, a-Si, oxide, nitride, III-V's

• Ashing

Photoresist removal

• Deposition (PECVD)

Oxide, nitride, a-Si

• Oxidation

Si

• Sputtering

Al, W, Au, Cu, YBaCuO

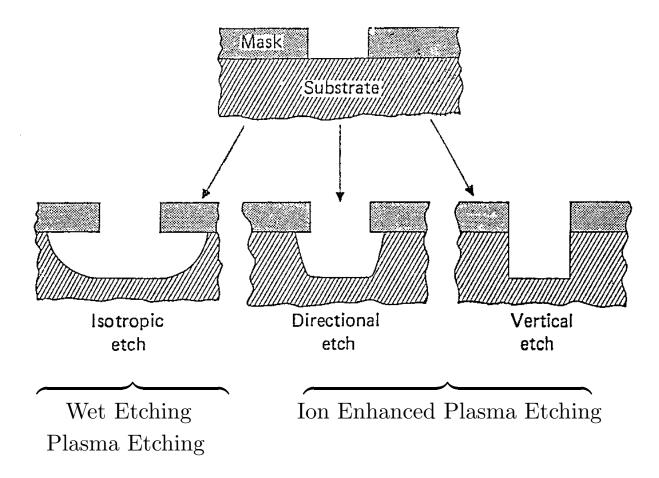
• Polymerization

Various plastics

• Implantation

H, He, B, P, O, As, Pd

ANISOTROPIC ETCHING



ISOTROPIC PLASMA ETCHING

- 1. Start with inert molecular gas CF₄
- 2. Make discharge to create reactive species:

$$CF_4 \longrightarrow CF_3 + F$$

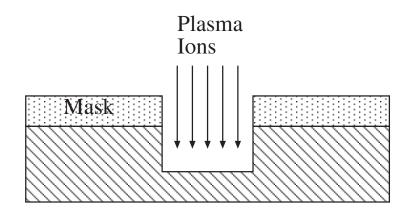
3. Species reacts with material, yielding volatile product:

$$Si + 4F \longrightarrow SiF_4 \uparrow$$

- 4. Pump away product
- 5. CF₄ does not react with Si; SiF₄ is volatile

ANISOTROPIC PLASMA ETCHING

- 6. Energetic ions bombard trench bottom, but not sidewalls:
 - (a) Increase etching reaction rate at trench bottom
 - (b) Clear passivating films from trench bottom



UNITS AND CONSTANTS

- SI units: meters (m), kilograms (kg), seconds (s), coulombs (C) $e = 1.6 \times 10^{-19}$ C, electron charge = -e
- Energy unit is joule (J)
 Often use electron-volt

$$1 \text{ eV} = 1.6 \times 10^{-19} \text{ J}$$

• Temperature unit is kelvin (K)

Often use equivalent voltage of the temperature:

$$T_e(\text{volts}) = \frac{kT_e(\text{kelvins})}{e}$$

where $k = \text{Boltzmann's constant} = 1.38 \times 10^{-23} \text{ J/K}$

$$\boxed{1~\mathrm{V} \Longleftrightarrow 11,600~\mathrm{K}}$$

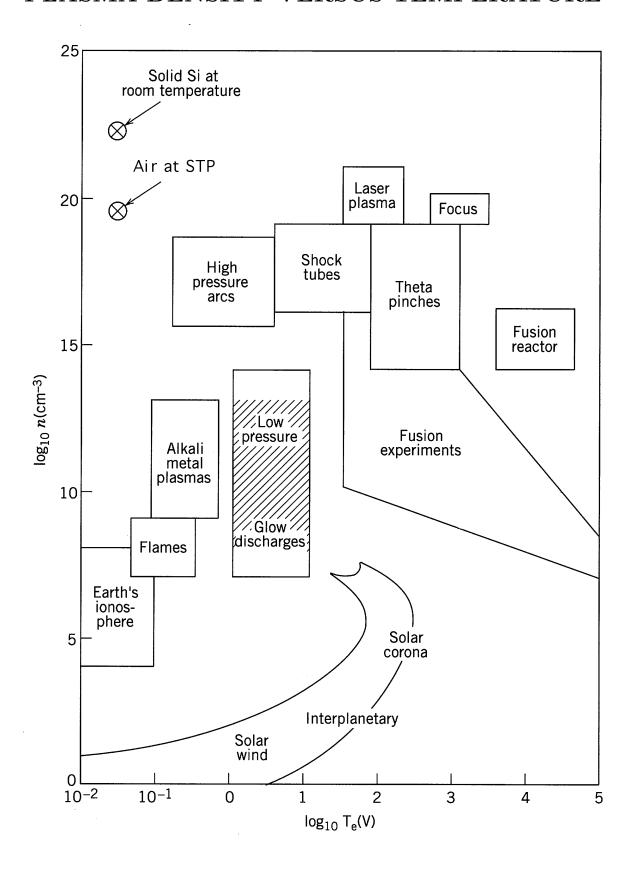
• Pressure unit is pascals (Pa); $1 \text{ Pa} = 1 \text{ N/m}^2$ Atmospheric pressure $\approx 10^5 \text{ Pa} \equiv 1 \text{ bar}$ Often use English units for gas pressures Atmospheric pressure = 760 Torr

$$1 \text{ Pa} \iff 7.5 \text{ mTorr}$$

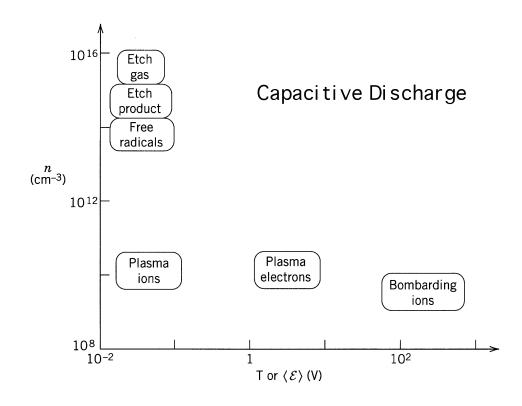
PHYSICAL CONSTANTS AND CONVERSION FACTORS

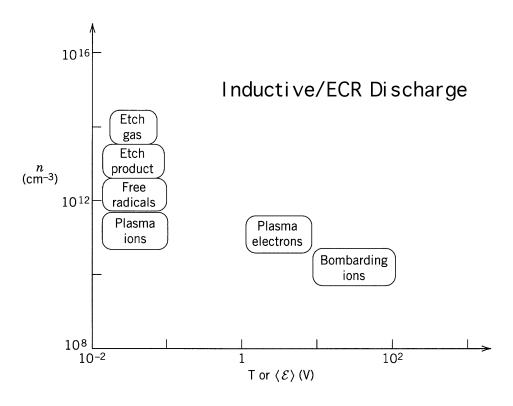
Quantity	Symbol	Value
Boltzmann constant Elementary charge Electron mass Proton mass Proton/electron mass ratio Planck constant	k e m M M/m h $\hbar = h/2\pi$	$1.3807 \times 10^{-23} \text{ J/K}$ $1.6022 \times 10^{-19} \text{ C}$ $9.1095 \times 10^{-31} \text{ kg}$ $1.6726 \times 10^{-27} \text{ kg}$ 1836.2 $6.6262 \times 10^{-34} \text{ J-s}$ $1.0546 \times 10^{-34} \text{ J-s}$
Speed of light in vacuum Permittivity of free space Permeability of free space Bohr radius Atomic cross section Temperature Temperature	c_0 ϵ_0 μ_0 $a_0 = 4\pi\epsilon_0 \hbar^2 / e^2 m$ πa_0^2	$2.9979 \times 10^{8} \text{ m/s}$ $8.8542 \times 10^{-12} \text{ F/m}$ $4\pi \times 10^{-7} \text{ H/m}$ $5.2918 \times 10^{-11} \text{ m}$ $8.7974 \times 10^{-21} \text{ m}^{2}$
Temperature T associated with $T = 1 \text{ V}$ Energy associated with $\mathcal{E} = 1 \text{ V}$ Avogadro number		11605 K $1.6022 \times 10^{-19} \text{ J}$
(molecules/mol) Gas constant Atomic mass unit Standard temperature	$ \begin{array}{l} N_A \\ R = kN_A \end{array} $	6.0220×10^{23} 8.3144 J/K-mol $1.6606 \times 10^{-27} \text{ kg}$
(25 °C) Standard pressure (760 Torr = 1 atm) Loschmidt's number	T_0 $p^{\scriptscriptstyle igoreau}$	298.15 K $1.0133 \times 10^5 \text{ Pa}$
(density at STP) Pressure of 1 Torr Energy per mole at T_0 calorie (cal)	n° RT_0	$2.6868 \times 10^{25} \text{ m}^{-3}$ 133.32 Pa 2.4789 kJ/mol 4.1868 J

PLASMA DENSITY VERSUS TEMPERATURE



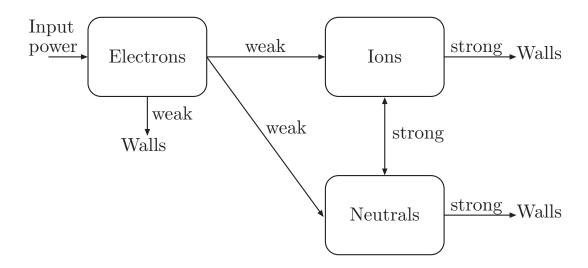
RELATIVE DENSITIES AND ENERGIES





NON-EQUILIBRIUM

• Energy coupling between electrons and heavy particles is weak



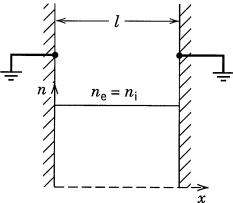
• Electrons are *not* in thermal equilibrium with ions or neutrals

 $T_e \gg T_i$ in plasma bulk Bombarding $\mathcal{E}_i \gg \mathcal{E}_e$ at wafer surface

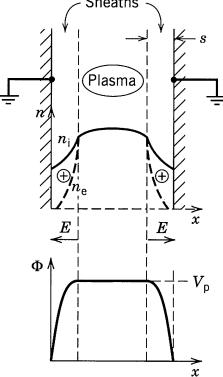
- "High temperature processing at low temperatures"
 - 1. Wafer can be near room temperature
 - 2. Electrons produce free radicals \Longrightarrow chemistry
 - 3. Electrons produce electron-ion pairs \Longrightarrow ion bombardment

ELEMENTARY DISCHARGE BEHAVIOR

• Consider uniform density of electrons and ions n_e and n_i at time t=0

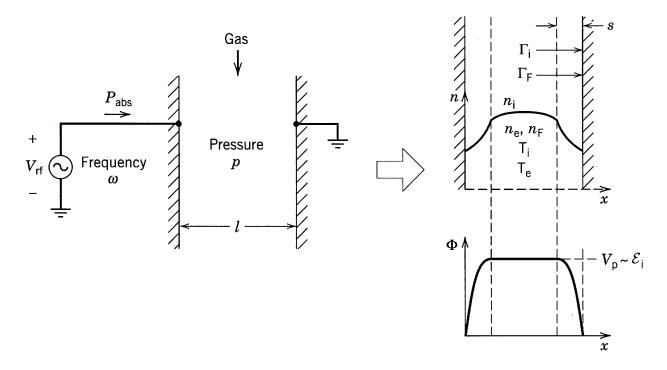


• Warm electrons having low mass quickly drain to the wall, setting up sheaths



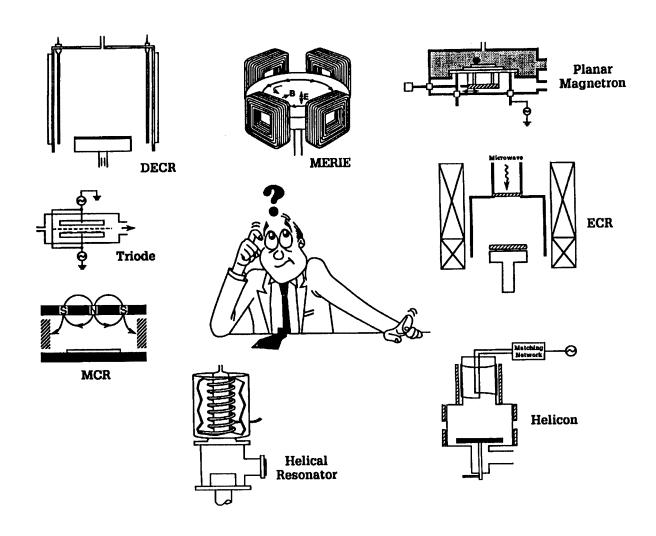
• Ions accelerated to walls; ion bombarding energy $\mathcal{E}_i = \text{plasmawall potential } V_p$

CENTRAL PROBLEM IN DISCHARGE MODELING



- Given $V_{\rm rf}$ (or $I_{\rm rf}$ or $P_{\rm rf}$), ω , gases, pressure, flow rates, discharge geometry $(R, l, {\rm etc})$, then
- Find plasma densities n_e , n_i , temperatures T_e , T_i , ion bombarding energies \mathcal{E}_i , sheath thicknesses, neutral radical densities, potentials, currents, fluxes, etc
- Learn how to design and optimize plasma reactors for various purposes (etching, deposition, etc)

CHOOSING PLASMA PROCESSING EQUIPMENT



• How about inductive? (figure published in 1991)

SUMMARY OF PLASMA FUNDAMENTALS

POISSON'S EQUATION

• An electric field can be generated by charges:

$$\nabla \cdot \mathbf{E} = \frac{\rho}{\epsilon_0}$$
 or $\iint_S \bar{\mathbf{E}} \cdot d\mathbf{A} = \frac{Q_{\text{encl}}}{\epsilon_0}$

• For slow time variations (dc, rf, but not microwaves):

$$\mathbf{E} = -\nabla \Phi$$

Combining these yields Poisson's equation:

$$\nabla^2 \Phi = -\frac{\rho}{\epsilon_0}$$

- Here $\mathbf{E} = \text{electric field (V/m)}, \ \rho = \text{charge density (C/m}^3),$ $\Phi = \text{potential (V)}$
- In 1D:

$$\frac{dE_x}{dx} = \frac{\rho}{\epsilon_0}, \qquad E_x = -\frac{d\Phi}{dx}$$

yields

$$\frac{d^2\Phi}{dx^2} = -\frac{\rho}{\epsilon_0}$$

• This field powers a capacitive discharge or the wafer bias power of an inductive or ECR discharge $V_{\rm rf} \ominus \begin{array}{c} & & & \\$

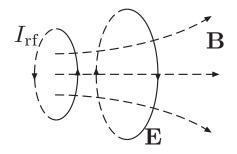
FARADAY'S LAW

• An electric field can be generated by a time-varying magnetic field:

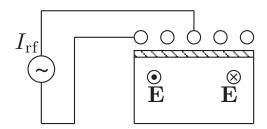
$$\nabla \times \mathbf{E} = -\frac{\partial \mathbf{B}}{\partial t}$$

or

$$\oint_{\mathcal{C}} \mathbf{E} \cdot d\mathbf{l} = -\frac{\partial}{\partial t} \iint_{\mathcal{A}} \mathbf{B} \cdot d\mathbf{A}$$



- Here $\mathbf{B} = \text{magnetic induction vector}$
- This field powers the coil of an inductive discharge (top power)



AMPERE'S LAW

• Both conduction currents and displacement currents generate magnetic fields:

$$\nabla \times \mathbf{H} = \mathbf{J}_c + \epsilon_0 \frac{\partial \mathbf{E}}{\partial t} = \mathbf{J}_T$$

- \mathbf{J}_c = conduction current, $\epsilon_0 \partial \mathbf{E}/\partial t$ = displacement current, \mathbf{J}_T = total current, \mathbf{H} = magnetic field vector, $\mathbf{B} = \mu_0 \mathbf{H}$ with $\mu_0 = 4\pi \times 10^{-6} \text{ H/m}$
- Note the vector identity:

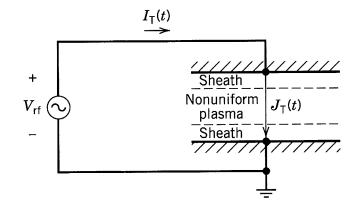
$$\nabla \cdot (\nabla \times \mathbf{H}) = 0 \qquad \Rightarrow \qquad \nabla \cdot \mathbf{J}_T = 0$$

• In 1D:

$$\frac{\partial J_{Tx}(x,\,t)}{\partial x} = 0$$

SO

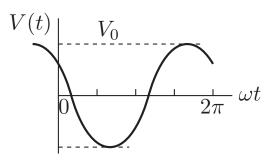
$$J_{Tx} = J_{Tx}(t)$$
, independent of x



REVIEW OF PHASORS

• Physical voltage (or current), a real sinusoidal function of time

$$V(t) = V_0 \cos(\omega t + \phi)$$



• Phasor voltage (or current), a complex number, independent of time $V_{I|}$

$$\tilde{V} = V_0 e^{j\phi} = V_R + jV_I$$

 V_{I} V_{0} ϕ V_{R}

• Using $e^{j\phi} = \cos \phi + j \sin \phi$, we find

$$V_R = V_0 \cos \phi, \qquad V_I = V_0 \sin \phi$$

• Note that

$$V(t) = \operatorname{Re}\left(\tilde{V} e^{j\omega t}\right)$$

$$= V_0 \cos(\omega t + \phi)$$

$$= V_R \cos \omega t - V_I \sin \omega t$$

• Hence

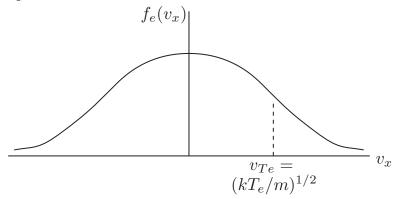
$$V(t) \iff \tilde{V}$$
 (given ω)

THERMAL EQUILIBRIUM PROPERTIES

- Electrons generally near thermal equilibrium Ions generally not in thermal equilibrium
- Maxwellian distribution of electrons

$$f_e(v) = n_e \left(\frac{m}{2\pi k T_e}\right)^{3/2} \exp\left(-\frac{mv^2}{2k T_e}\right)$$

where $v^2 = v_x^2 + v_y^2 + v_z^2$



• Pressure p = nkT

For neutral gas at room temperature (300 K)

$$n_g(\mathrm{cm}^{-3}) \approx 3.3 \times 10^{16} \, p(\mathrm{Torr})$$

AVERAGES OVER MAXWELLIAN DISTRIBUTION

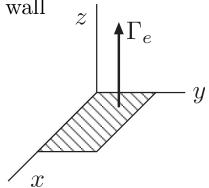
• Average energy

$$\langle \frac{1}{2}mv^2 \rangle = \frac{1}{n_e} \int d^3v \frac{1}{2}mv^2 f_e(v) = \frac{3}{2}kT_e$$

• Average speed

$$\bar{v}_e = \frac{1}{n_e} \int d^3v \, v f_e(v) = \left[\left(\frac{8kT_e}{\pi m} \right)^{1/2} \right]$$

• Average electron flux lost to a wall



$$\Gamma_e = \int_{-\infty}^{\infty} dv_x \int_{-\infty}^{\infty} dv_y \int_{0}^{\infty} dv_z v_z f_e(v) = \boxed{\frac{1}{4} n_e \bar{v}_e} \quad [\text{m}^{-2}\text{-s}^{-1}]$$

• Average kinetic energy lost per electron lost to a wall

$$\mathcal{E}_e = 2 \, \mathrm{T}_e$$

FORCES ON PARTICLES

• For a unit volume of electrons (or ions),

$$mn_e \frac{d\mathbf{u}_e}{dt} = qn_e \mathbf{E} - \nabla p_e - mn_e \nu_m \mathbf{u}_e$$

 $mass \times acceleration = electric field force +$

+ pressure gradient force + friction (gas drag) force

• m = electron mass

 $n_e = \text{electron density}$

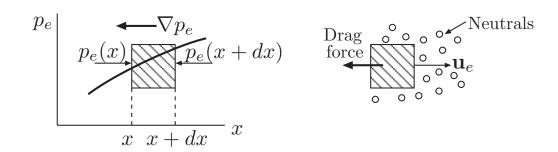
 $\mathbf{u}_e = \text{electron flow velocity}$

q = -e for electrons (+e for ions)

 $\mathbf{E} = \text{electric field}$

 $p_e = n_e k T_e = \text{electron pressure}$

 ν_m = collision frequency of electrons with neutrals



BOLTZMANN FACTOR FOR ELECTRONS

• If electric field and pressure gradient forces almost balance:

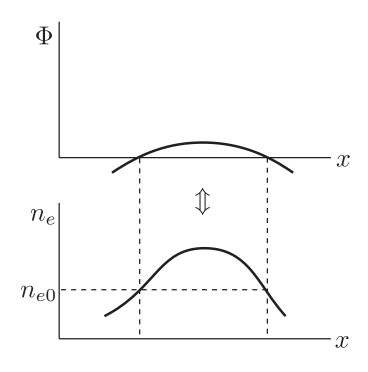
$$0 \approx -en_e \mathbf{E} - \nabla p_e$$

• Let $\mathbf{E} = -\nabla \Phi$ and $p_e = n_e k T_e$:

$$\nabla \Phi = \frac{kT_e}{e} \frac{\nabla n_e}{n_e}$$

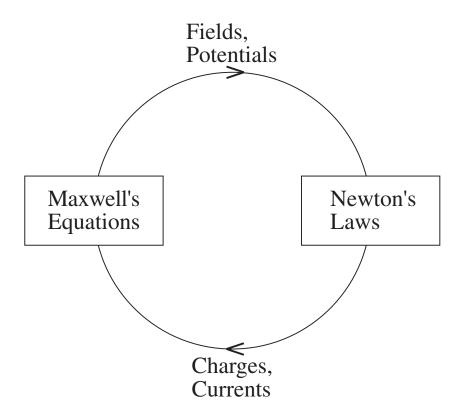
• Put $kT_e/e = T_e$ (volts) and integrate to obtain:

$$n_e(\mathbf{r}) = n_{e0} e^{\Phi(\mathbf{r})/T_e}$$



UNDERSTANDING PLASMA BEHAVIOR

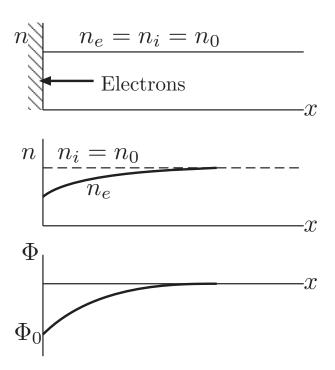
• The field equations and the force equations are coupled



DEBYE LENGTH λ_{De}

- The characteristic length scale of a plasma
- Low voltage sheaths \sim few Debye lengths thick
- Let's consider how a sheath forms near a wall:

 Electrons leave plasma before ions and charge wall negative



Assume electrons in thermal equilibrium and stationary ions

DEBYE LENGTH λ_{De} (CONT'D)

• Newton's laws

$$n_e(x) = n_0 e^{\Phi/T_e}, \qquad n_i = n_0$$

• Use in Poisson's equation

$$\frac{d^2\Phi}{dx^2} = -\frac{en_0}{\epsilon_0} \left(1 - e^{\Phi/T_e} \right)$$

• Linearize $e^{\Phi/T_e} \approx 1 + \Phi/T_e$

$$\frac{d^2\Phi}{dx^2} = \frac{en_0}{\epsilon_0 T_e} \Phi$$

• Solution is

$$\Phi(x) = \Phi_0 e^{-x/\lambda_{De}}, \qquad \lambda_{De} = \left(\frac{\epsilon_0 T_e}{e n_0}\right)^{1/2}$$

• In practical units

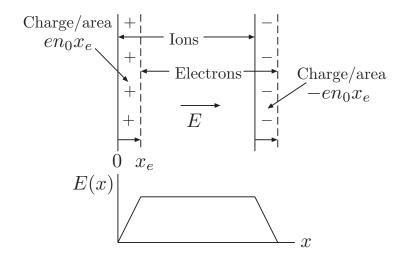
$$\lambda_{De}(\text{cm}) = 740\sqrt{\text{T}_e/n_0}, \quad \text{T}_e \text{ in volts}, n_0 \text{ in cm}^{-3}$$

• Example

At
$$T_e = 1$$
 V and $n_0 = 10^{10}$ cm⁻³, $\lambda_{De} = 7.4 \times 10^{-3}$ cm
 \Longrightarrow Sheath is ~ 0.15 mm thick (Very thin!)

ELECTRON PLASMA FREQUENCY ω_{pe}

- The fundamental timescale for a plasma
- Consider a plasma slab (no walls). Displace all electrons to the right a small distance x_{e0} , and release them:



• Maxwell's equations (parallel plate capacitor)

$$E = \frac{en_0 x_e(t)}{\epsilon_0}$$

• Newton's laws (electron motion)

$$m\frac{d^2x_e(t)}{dt^2} = -\frac{e^2n_0}{\epsilon_0}x_e(t)$$

• Solution is electron plasma oscillations

$$x_e(t) = x_{e0} \cos \omega_{pe} t,$$

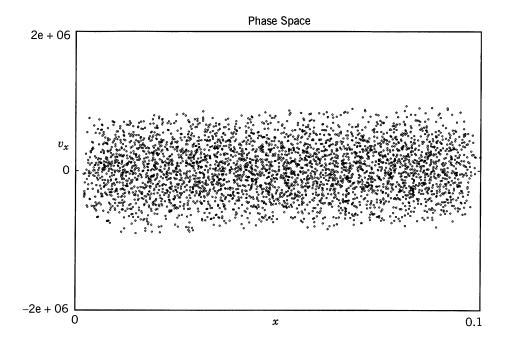
$$\omega_{pe} = \left(\frac{e^2 n_0}{\epsilon_0 m}\right)^{1/2}$$

• Practical formula is $f_{pe}(\mathrm{Hz}) = 9000\sqrt{n_0}$, n_0 in cm⁻³ \Longrightarrow microwave frequencies ($\gtrsim 1$ GHz) for typical plasmas

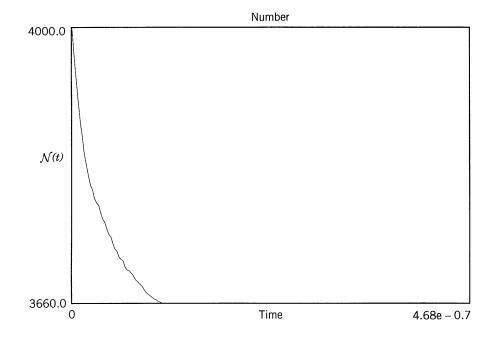
1D SIMULATION OF SHEATH FORMATION

$$(T_e = 1 \text{ V}, n_e = n_i = 10^{13} \text{ m}^{-3})$$

• Electron v_x -x phase space at $t = 0.77 \ \mu s$

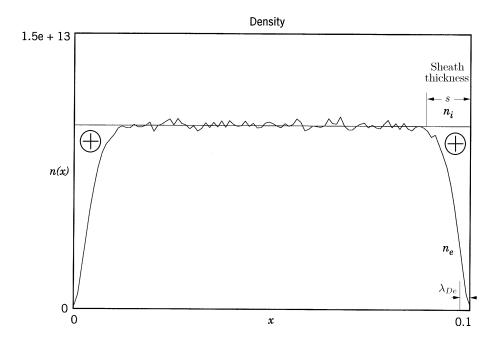


• Electron number $\mathcal N$ versus t

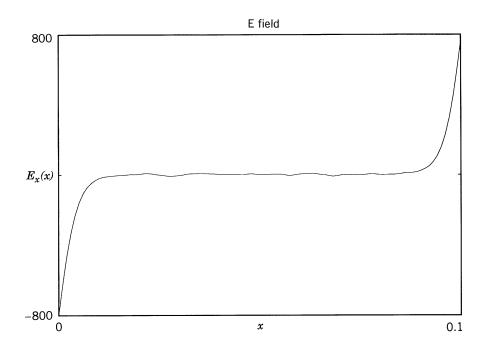


1D SIMULATION OF SHEATH FORMATION (CONT'D)

• Electron density $n_e(x)$ at $t = 0.77 \ \mu s$

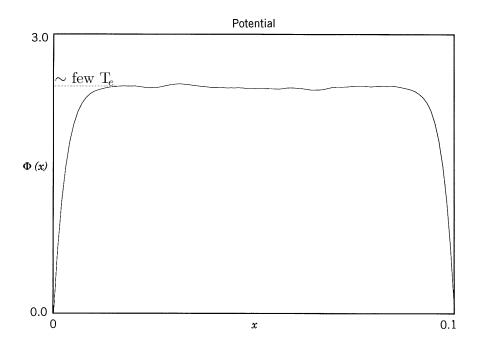


• Electric field E(x) at $t = 0.77 \ \mu s$

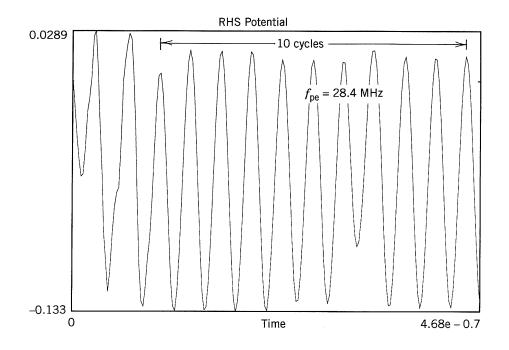


1D SIMULATION OF SHEATH FORMATION (CONT'D)

• Potential $\Phi(x)$ at $t = 0.77 \ \mu s$



• Right hand potential $\Phi(x=l)$ versus t



PLASMA DIELECTRIC CONSTANT $\epsilon_{\mathbf{p}}$

• RF discharges are driven at a frequency ω

$$E(t) = \operatorname{Re}(\tilde{E} e^{j\omega t}), \quad \text{etc}$$

• Define ϵ_p from the total current in Maxwell's equations

$$\nabla \times \tilde{H} = \underbrace{\tilde{J}_c + j\omega\epsilon_0 \tilde{E}}_{\text{Total current }} \equiv j\omega\epsilon_p \tilde{E}$$

- Conduction current $\tilde{J}_c = -en_e \tilde{u}_e$ is mainly due to electrons
- Newton's law (electric field and neutral drag) is

$$j\omega m\tilde{u}_e = -e\tilde{E} - m\nu_m\tilde{u}_e$$

• Solve for \tilde{u}_e and evaluate \tilde{J}_c to obtain

$$\epsilon_p = \epsilon_0 \left[1 - \frac{\omega_{pe}^2}{\omega(\omega - j\nu_m)} \right]$$

• For $\omega \gg \nu_m$, ϵ_p is mainly real (nearly lossless dielectric)

For $\nu_m \gg \omega$, ϵ_p is mainly imaginary (very lossy dielectric)

RF FIELDS IN LOW PRESSURE DISCHARGES

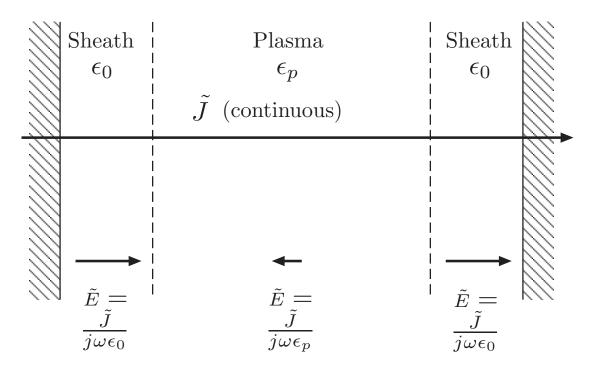
• Consider mainly lossless plasma $(\omega \gg \nu_m)$

$$\epsilon_p = \epsilon_0 \left(1 - \frac{\omega_{pe}^2}{\omega^2} \right)$$

• For almost all RF discharges, $\omega_{pe} \gg \omega$

$$\Longrightarrow \epsilon_p$$
 is negative

• Typical case: $\epsilon_p = -1000 \,\epsilon_0$



- Electric field in plasma is $1000 \times \text{smaller than in sheaths!}$
- Although field in plasma is small, it sustains the plasma!

PLASMA CONDUCTIVITY $\sigma_{\mathbf{p}}$

- Useful to introduce the plasma conductivity $\tilde{J}_c \equiv \sigma_p \tilde{E}$
- RF plasma conductivity

$$\sigma_p = \frac{e^2 n_e}{m(\nu_m + j\omega)}$$

• DC plasma conductivity ($\omega \ll \nu_m$)

$$\sigma_{\rm dc} = \frac{e^2 n_e}{m \nu_m}$$

• The plasma dielectric constant and conductivity are related by:

$$j\omega\epsilon_p = \sigma_p + j\omega\epsilon_0$$

• Due to σ_p , rf current flowing through the plasma heats electrons (just like a resistor)

OHMIC HEATING POWER

• Time average power absorbed/volume

$$p_d = \langle \mathbf{J}(t) \cdot \mathbf{E}(t) \rangle = \frac{1}{2} \operatorname{Re} \left(\tilde{J} \cdot \tilde{E}^* \right) \qquad [\text{W/m}^3]$$

• Put $\tilde{J} = (\sigma_p + j\omega\epsilon_0)\tilde{E}$ to find p_d in terms of \tilde{E}

$$p_d = \frac{1}{2} |\tilde{E}|^2 \sigma_{\rm dc} \frac{\nu_m^2}{\omega^2 + \nu_m^2}$$

• Put $\tilde{E} = \tilde{J}/(\sigma_p + j\omega\epsilon_0)$ to find p_d in terms of \tilde{J} . For almost all rf discharges $(\omega_{pe} \gg \omega)$

$$p_d = \frac{1}{2} |\tilde{J}|^2 \frac{1}{\sigma_{\rm dc}}$$

SUMMARY OF DISCHARGE FUNDAMENTALS

ELECTRON COLLISIONS WITH ARGON

• Maxwellian electrons collide with Ar atoms (density n_g)

$$\frac{dn_e}{dt} = \nu n_e = K n_g \, n_e$$

 $\nu = \text{collision frequency [s}^{-1}], K(T_e) = \text{rate coefficient [m}^3/\text{s}]$

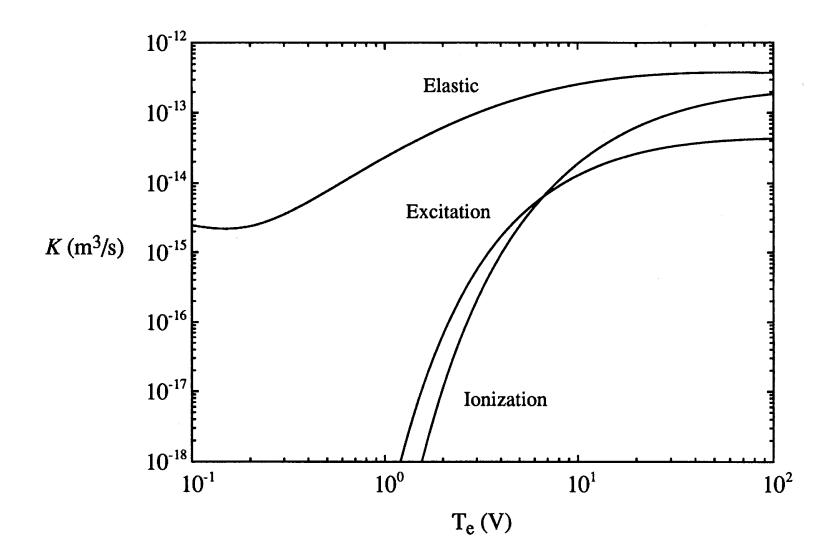
• Electron-Ar collision processes

$$e + Ar \longrightarrow Ar^{+} + 2e$$
 (ionization)
 $e + Ar \longrightarrow e + Ar^{*} \longrightarrow e + Ar + photon$ (excitation)
 $e + Ar \longrightarrow e + Ar$ (elastic scattering)

• Rate coefficient $K(T_e)$ is average of cross section σ [m²] for process, over Maxwellian distribution

$$K(T_e) = \langle \sigma v \rangle_{\text{Maxwellian}}$$

ELECTRON-ARGON RATE COEFFICIENTS



ION COLLISIONS WITH ARGON

• Argon ions collide with Ar atoms

$$Ar^{+} + Ar \longrightarrow Ar^{+} + Ar$$
 (elastic scattering)



$$Ar^{+} + Ar \longrightarrow Ar + Ar^{+}$$
 (charge transfer)



- Total cross section for room temperature ions $\sigma_i \approx 10^{-14} \text{ cm}^2$
- Ion-neutral mean free path

$$\lambda_i = \frac{1}{n_g \sigma_i}$$

• Practical formula

$$\lambda_i(\text{cm}) = \frac{1}{330 \, p}, \qquad p \text{ in Torr}$$

• Rate coefficient for ion-neutral collisions

$$K_i = \frac{\bar{v}_i}{\lambda_i}$$

with
$$\bar{v}_i = (8kT_i/\pi M)^{1/2}$$

THREE ENERGY LOSS PROCESSES

1. Collisional energy \mathcal{E}_c lost per electron-ion pair created

$$K_{iz}\mathcal{E}_c = K_{iz}\mathcal{E}_{iz} + K_{ex}\mathcal{E}_{ex} + K_{el}(2m/M)(3T_e/2)$$

$$\Longrightarrow \mathcal{E}_c(T_e) \qquad \text{(voltage units)}$$

 \mathcal{E}_{iz} , \mathcal{E}_{ex} , and $(3m/M)T_e$ are energies lost by an electron due to an ionization, excitation, and elastic scattering collision

2. Electron kinetic energy lost to walls

$$\mathcal{E}_e = 2 \, \mathrm{T}_e$$

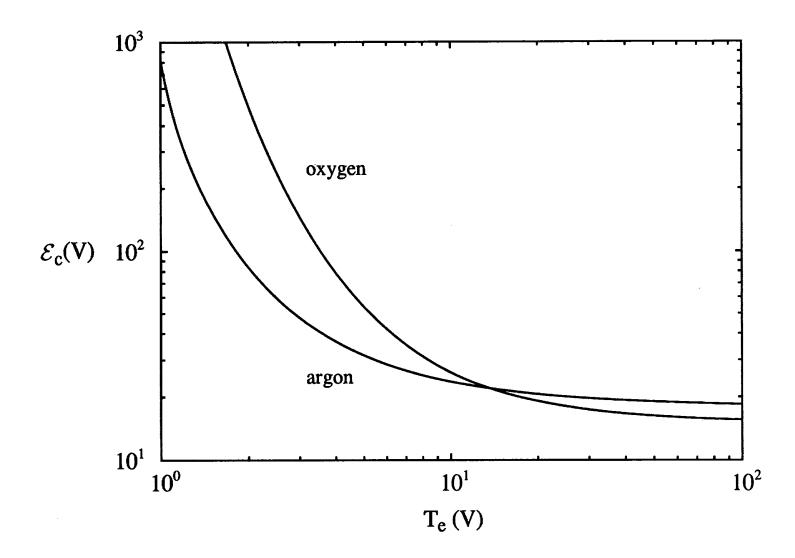
3. Ion kinetic energy lost to walls is mainly due to the dc potential \bar{V}_s across the sheath

$$\mathcal{E}_i \approx \bar{V}_s$$

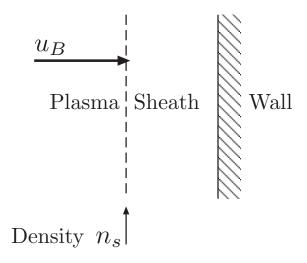
• Total energy lost per electron-ion pair lost to walls

$$\mathcal{E}_T = \mathcal{E}_c + \mathcal{E}_e + \mathcal{E}_i$$

COLLISIONAL ENERGY LOSSES



BOHM (ION LOSS) VELOCITY u_B



• Due to formation of a "presheath", ions arrive at the plasmasheath edge with directed energy $kT_e/2$

$$\frac{1}{2}Mu_i^2 = \frac{kT_e}{2}$$

• At the plasma-sheath edge (density n_s), electron-ion pairs are lost at the Bohm velocity

$$u_i = u_B = \left(\frac{kT_e}{M}\right)^{1/2}$$

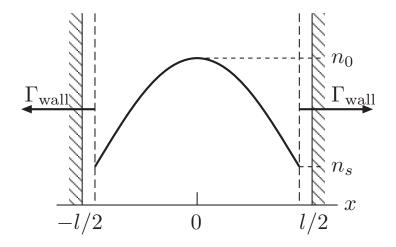
AMBIPOLAR DIFFUSION AT HIGH PRESSURES

- Plasma bulk is quasi-neutral $(n_e \approx n_i = n)$ and the electron and ion loss fluxes are equal $(\Gamma_e \approx \Gamma_i \approx \Gamma)$
- Fick's law

$$\Gamma = -D_a \nabla n$$

with ambipolar diffusion coefficient $D_a = kT_e/M\nu_i$

• Density profile is sinusoidal



• Loss flux to the wall is

$$\Gamma_{\text{wall}} = h_l n_0 u_B$$

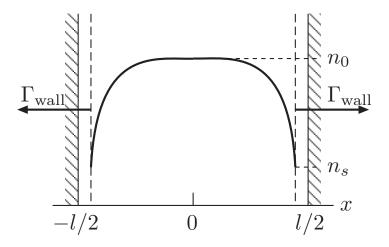
where the edge-to-center density ratio is

$$h_l \equiv \frac{n_s}{n_0} = \frac{\pi}{l} \frac{u_B}{\nu_i}$$

 \bullet Applies for pressures > 100 mTorr in argon

AMBIPOLAR DIFFUSION AT LOW PRESSURES

- The diffusion coefficient is not constant
- Density profile is relatively flat in the center and falls sharply near the sheath edge



• For a cylindrical plasma of length l and radius R, loss fluxes to axial and radial walls are

$$\Gamma_{\text{axial}} = h_l n_0 u_B, \qquad \Gamma_{\text{radial}} = h_R n_0 u_B$$

where the edge-to-center density ratios are

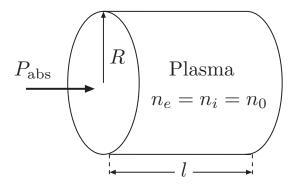
$$h_l \approx \frac{0.86}{(3+l/2\lambda_i)^{1/2}}, \qquad h_R \approx \frac{0.8}{(4+R/\lambda_i)^{1/2}}$$

• Applies for pressures < 100 mTorr in argon

ANALYSIS OF DISCHARGE EQUILIBRIUM

PARTICLE BALANCE AND T_e

• Assume uniform cylindrical plasma absorbing power $P_{\rm abs}$



• Particle balance

Production due to ionization = loss to the walls

$$K_{iz}n_g n_0 \pi R^2 l = (2\pi R^2 h_l n_0 + 2\pi R l h_R n_0) u_B$$

• Solve to obtain

$$\frac{K_{\rm iz}(T_e)}{u_B(T_e)} = \frac{1}{n_g d_{\rm eff}}$$

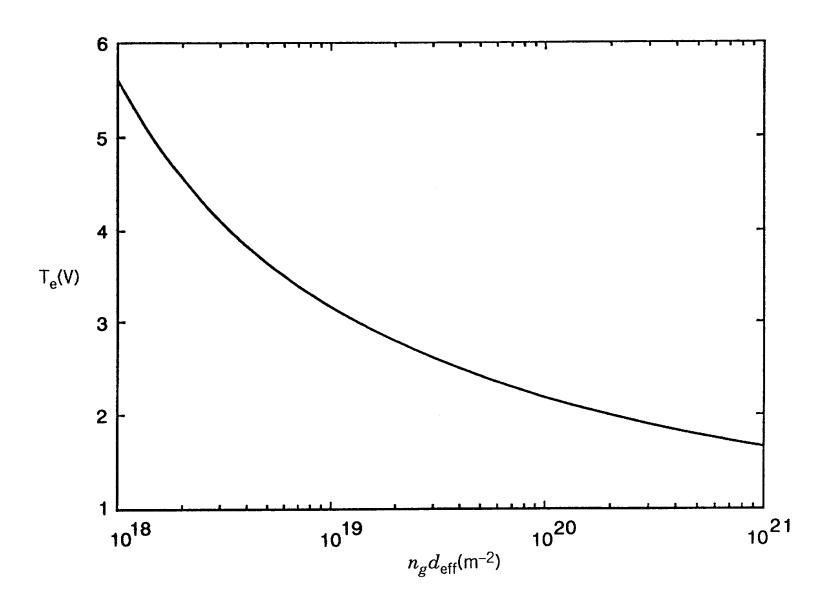
where

$$d_{\text{eff}} = \frac{1}{2} \frac{Rl}{Rh_l + lh_R}$$

is an effective plasma size

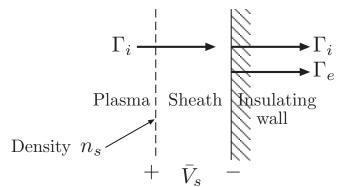
- Given n_g and $d_{\text{eff}} \Longrightarrow \text{electron temperature } T_e$
- T_e varies over a narrow range of 2–5 volts

ELECTRON TEMPERATURE IN ARGON DISCHARGE



ION ENERGY FOR LOW VOLTAGE SHEATHS

- \mathcal{E}_i = energy entering sheath + energy gained traversing sheath
- Ion energy entering sheath = $T_e/2$ (voltage units)
- Sheath voltage determined from particle conservation in the sheath



$$\Gamma_i = n_s u_B, \qquad \Gamma_e = \frac{1}{4} n_s \bar{v}_e e^{-\bar{V}_s/T_e}$$

with $\bar{v}_e = (8eT_e/\pi m)^{1/2}$

• The ion and electron fluxes must balance

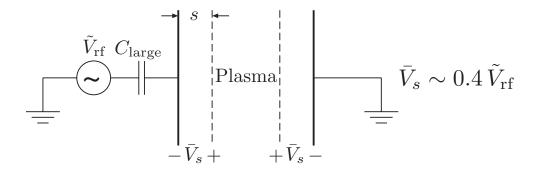
$$oxed{ar{V}_s = rac{ ext{T}_e}{2} \, \ln\left(rac{M}{2\pi m}
ight)}$$

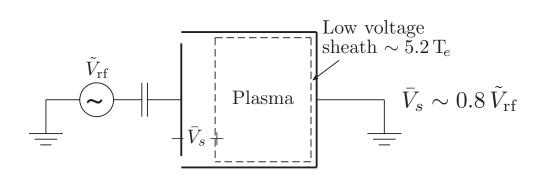
or $\bar{V}_s \approx 4.7 \, \mathrm{T}_e$ for argon

• Accounting for the initial ion energy, $\mathcal{E}_i \approx 5.2 \, \mathrm{T}_e$

ION ENERGY FOR HIGH VOLTAGE SHEATHS

• Large ion bombarding energies can be gained near rf-driven electrodes embedded in the plasma





 \bullet The sheath thickness s is given by the Child Law

$$\bar{J}_i = e n_s u_B = \frac{4}{9} \epsilon_0 \left(\frac{2e}{M}\right)^{1/2} \frac{\bar{V}_s^{3/2}}{s^2}$$

• Estimating ion energy is not simple as it depends on the type of discharge and the application of bias voltages

POWER BALANCE AND n₀

• Assume low voltage sheaths at all surfaces

$$\mathcal{E}_T(T_e) = \underbrace{\mathcal{E}_c(T_e)}_{\text{Collisional Electron}} + \underbrace{2 T_e}_{\text{Lon}} + \underbrace{5.2 T_e}_{\text{Lon}}$$

• Power balance

Power in = power out

$$P_{\text{abs}} = (h_l n_0 2\pi R^2 + h_R n_0 2\pi R l) u_B e \mathcal{E}_T$$

• Solve to obtain

$$n_0 = \frac{P_{\rm abs}}{A_{\rm eff} u_B e \mathcal{E}_T}$$

where

$$A_{\text{eff}} = 2\pi R^2 h_l + 2\pi R l h_R$$

is an effective area for particle loss

- Density n_0 is proportional to the absorbed power $P_{\rm abs}$
- Density n_0 depends on pressure p through h_l , h_R , and T_e

PARTICLE AND POWER BALANCE

• Particle balance \Longrightarrow electron temperature T_e (independent of plasma density)

• Power balance \Longrightarrow plasma density n_0 (once electron temperature T_e is known)

EXAMPLE 1

- Let R = 0.15 m, l = 0.3 m, $n_g = 3.3 \times 10^{19}$ m⁻³ (p = 1 mTorr at 300 K), and $P_{\text{abs}} = 800$ W
- Assume low voltage sheaths at all surfaces
- Find $\lambda_i = 0.03$ m. Then $h_l \approx h_R \approx 0.3$ and $d_{\text{eff}} \approx 0.17$ m
- From the T_e versus $n_g d_{\text{eff}}$ figure, T_e $\approx 3.5 \text{ V}$
- From the \mathcal{E}_c versus T_e figure, $\mathcal{E}_c \approx 42 \text{ V}$. Adding $\mathcal{E}_e = 2T_e \approx 7 \text{ V}$ and $\mathcal{E}_i \approx 5.2T_e \approx 18 \text{ V}$ yields $\mathcal{E}_T = 67 \text{ V}$
- Find $u_B \approx 2.9 \times 10^3$ m/s and find $A_{\rm eff} \approx 0.13$ m²
- Power balance yields $n_0 \approx 2.0 \times 10^{17} \text{ m}^{-3}$
- Ion current density $J_{il} = eh_l n_0 u_B \approx 2.9 \text{ mA/cm}^2$
- Ion bombarding energy $\mathcal{E}_i \approx 18 \text{ V}$

EXAMPLE 2

- Apply a strong dc magnetic field along the cylinder axis
 particle loss to radial wall is inhibited
- For no radial loss, $d_{\rm eff} = l/2h_l \approx 0.5 \text{ m}$
- From the T_e versus $n_g d_{\text{eff}}$ figure, $T_e \approx 3.3 \text{ V}$
- From the \mathcal{E}_c versus T_e figure, $\mathcal{E}_c \approx 46$ V. Adding $\mathcal{E}_e = 2T_e \approx 6.6$ V and $\mathcal{E}_i \approx 5.2T_e \approx 17$ V yields $\mathcal{E}_T = 70$ V
- Find $u_B \approx 2.8 \times 10^3$ m/s and find $A_{\rm eff} = 2\pi R^2 h_l \approx 0.043$ m²
- Power balance yields $n_0 \approx 5.8 \times 10^{17} \text{ m}^{-3}$
- Ion current density $J_{il} = eh_l n_0 u_B \approx 7.8 \text{ mA/cm}^2$
- Ion bombarding energy $\mathcal{E}_i \approx 17 \text{ V}$
 - \implies Significant increase in plasma density n_0

ELECTRON HEATING MECHANISMS

- Discharges can be distinguished by electron heating mechanisms
- (a) Ohmic (collisional) heating (capacitive, inductive discharges)
- (b) Stochastic (collisionless) heating (capacitive, inductive discharges)
- (c) Resonant wave-particle interaction heating (Electron cyclotron resonance and helicon discharges)
 - Achieving adequate electron heating is a central issue
 - Although the heated electrons provide the ionization required to sustain the discharge, the electrons tend to short out the applied heating fields within the bulk plasma

INDUCTIVE DISCHARGES

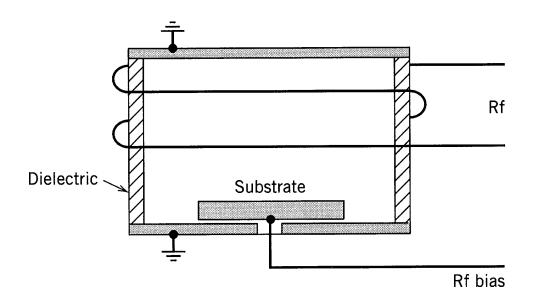
DESCRIPTION AND MODEL

MOTIVATION

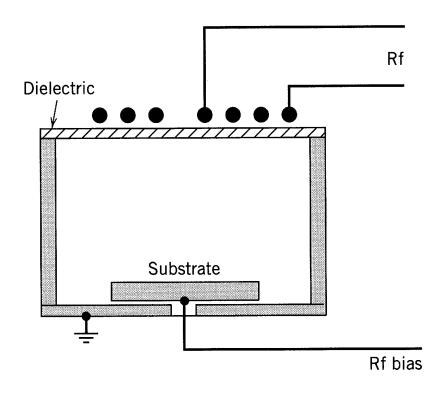
- Independent control of plasma density and ion energy
- Simplicity of concept
- RF rather than microwave powered
- No source magnetic fields

CYLINDRICAL AND PLANAR CONFIGURATIONS

ullet Cylindrical coil

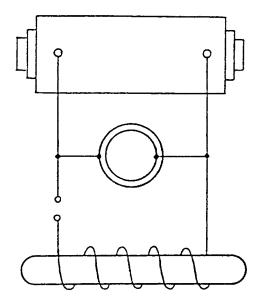


• Planar coil

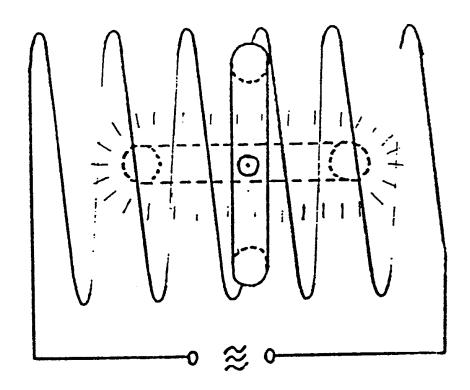


EARLY HISTORY

• First inductive discharge by Hittorf (1884)

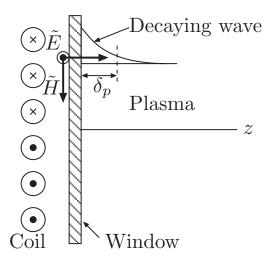


• Arrangement to test discharge mechanism by Lehmann (1892)



HIGH DENSITY REGIME

• Inductive coil launches electromagnetic wave into plasma



• Wave decays exponentially into plasma

$$\tilde{E} = \tilde{E}_0 e^{-z/\delta_p}, \qquad \delta_p = \frac{c}{\omega} \frac{1}{\operatorname{Im}(\kappa_p^{1/2})}$$

where κ_p = plasma dielectric constant

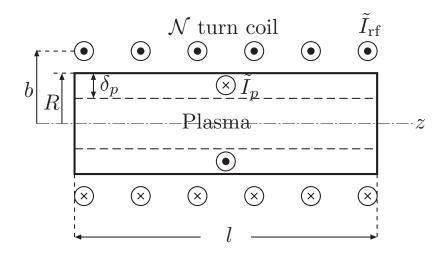
$$\kappa_p = 1 - \frac{\omega_{pe}^2}{\omega(\omega - j\nu_m)}$$

For typical high density, low pressure $(\nu_m \ll \omega)$ discharge

$$\delta_p \approx \frac{c}{\omega_{pe}} = \left(\frac{m}{e^2 \mu_0 n_e}\right)^{1/2} \sim 1-2 \text{ cm}$$

TRANSFORMER MODEL

• For simplicity consider long cylindrical discharge



 \bullet Current $\tilde{I}_{\rm rf}$ in ${\mathcal N}$ turn coil induces current \tilde{I}_p in 1-turn plasma skin

 \implies A transformer

PLASMA RESISTANCE AND INDUCTANCE

• Plasma resistance R_p

$$R_p = \frac{1}{\sigma_{\rm dc}} \frac{\text{circumference of plasma loop}}{\text{cross sectional area of loop}}$$

where

$$\sigma_{\rm dc} = \frac{e^2 n_{es}}{m \nu_m}$$

$$\Longrightarrow R_p = \frac{2\pi R}{\sigma_{\rm dc} l \delta_p}$$

• Plasma inductance L_p

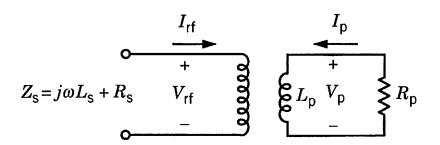
$$L_p = \frac{\text{magnetic flux produced by plasma current}}{\text{plasma current}}$$

• Using magnetic flux = $\pi R^2 \mu_0 \tilde{I}_p / l$

$$\implies L_p = \frac{\mu_0 \pi R^2}{l}$$

COUPLING OF PLASMA AND COIL

• Model the source as a transformer



$$\tilde{V}_{\rm rf} = j\omega L_{11}\tilde{I}_{\rm rf} + j\omega L_{12}\tilde{I}_{p}$$
$$\tilde{V}_{p} = j\omega L_{21}\tilde{I}_{\rm rf} + j\omega L_{22}\tilde{I}_{p}$$

• Transformer inductances

$$L_{11} = \frac{\text{magnetic flux linking coil}}{\text{coil current}} = \frac{\mu_0 \pi b^2 \mathcal{N}^2}{l}$$

$$L_{12} = L_{21} = \frac{\text{magnetic flux linking plasma}}{\text{coil current}} = \frac{\mu_0 \pi R^2 \mathcal{N}}{l}$$

$$L_{22} = L_p = \frac{\mu_0 \pi R^2}{l}$$

• Put $\tilde{V}_p = -\tilde{I}_p R_p$ in transformer equations and solve for impedance $Z_s = \tilde{V}_{\rm rf}/\tilde{I}_{\rm rf}$ seen at coil terminals

$$Z_s = j\omega L_{11} + \frac{\omega^2 L_{12}^2}{R_p + j\omega L_p}$$

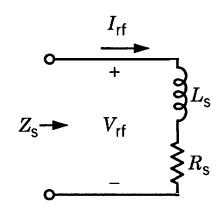
SOURCE CURRENT AND VOLTAGE

• Equivalent circuit at coil terminals

$$Z_s = R_s + j\omega L_s$$

$$R_s = \mathcal{N}^2 \frac{2\pi R}{\sigma_{\rm dc} l \delta_p}$$

$$L_s = \frac{\mu_0 \pi R^2 \mathcal{N}^2}{l} \left(\frac{b^2}{R^2} - 1\right)$$



ullet Power balance $\Longrightarrow \tilde{I}_{\mathrm{rf}}$

$$P_{\rm abs} = \frac{1}{2}\tilde{I}_{\rm rf}^2 R_s$$

• From source impedance $\Longrightarrow V_{\rm rf}$

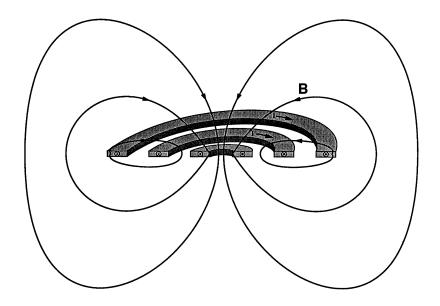
$$\tilde{V}_{\rm rf} = \tilde{I}_{\rm rf} Z_s$$

EXAMPLE

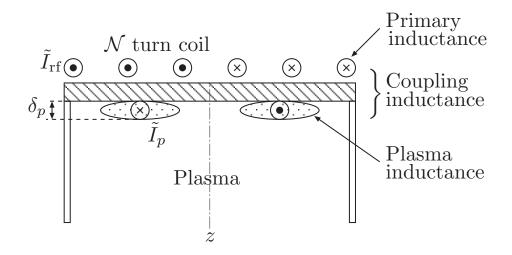
- Assume plasma radius R=10 cm, coil radius b=15 cm, length l=20 cm, $\mathcal{N}=3$ turns, gas density $n_g=1.7\times 10^{14}$ cm⁻³ (5 mTorr argon at 300 K), $\omega=85\times 10^6$ s⁻¹ (13.56 MHz), absorbed power $P_{\rm abs}=600$ W, and low voltage sheaths
- At 5 mTorr, $\lambda_i \approx 0.6$ cm, $h_l \approx h_R \approx 0.19$, and $d_{\text{eff}} \approx 17.9$ cm
- Particle balance (T_e versus $n_g d_{\text{eff}}$ figure) yields $T_e \approx 2.6 \text{ V}$
- Collisional energy losses (\mathcal{E}_c versus T_e figure) are $\mathcal{E}_c \approx 58 \text{ V}$ Adding $\mathcal{E}_e + \mathcal{E}_i = 7.2 T_e$ yields total energy losses $\mathcal{E}_T \approx 77 \text{ V}$
- $u_B \approx 2.5 \times 10^5 \text{ cm/s and } A_{\text{eff}} \approx 350 \text{ cm}^2$
- Power balance yields $n_e \approx 5.6 \times 10^{11} \ \mathrm{cm^{-3}}$ and $n_{se} \approx 1.0 \times 10^{11} \ \mathrm{cm^{-3}}$
- Use n_{se} to find skin depth $\delta_p \approx 1.7$ cm; estimate $\nu_m = K_{\rm el} n_g$ ($K_{\rm el}$ versus T_e figure) to find $\nu_m \approx 1.4 \times 10^7 \ {\rm s}^{-1}$
- Use ν_m and n_{se} to find $\sigma_{dc} \approx 113 \Omega^{-1}$ -m⁻¹
- Evaluate impedance elements $R_s \approx 14.7 \ \Omega$ and $L_s \approx 2.2 \ \mu\text{H}$; $|Z_s| \approx \omega L_s \approx 190 \ \Omega$
- Power balance yields $\tilde{I}_{\rm rf} \approx 9.0 {\rm A}$; from impedance $\tilde{V}_{\rm rf} \approx 1720 {\rm V}$

PLANAR COIL DISCHARGE

• Magnetic field produced by planar coil



• RF power is deposited in ring-shaped plasma volume



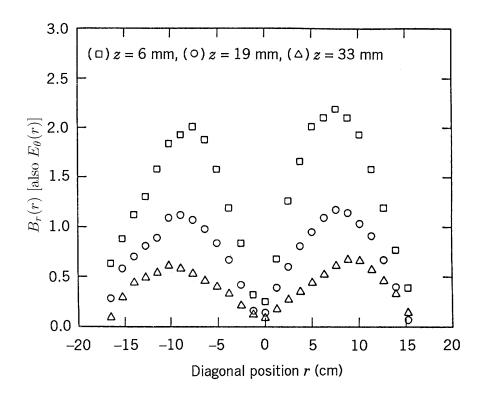
• As for a cylindrical discharge, there is a primary (L_{11}) , coupling $(L_{12} = L_{21})$ and secondary $(L_p = L_{22})$ inductance

PLANAR COIL FIELDS

• A ring-shaped plasma forms because

Induced electric field =
$$\begin{cases} 0, & \text{on axis} \\ \max, & \text{at } r \approx \frac{1}{2} R_{\text{wall}} \\ 0, & \text{at } r = R_{\text{wall}} \end{cases}$$

• Measured radial variation of B_r (and E_θ) at three distances below the window (5 mTorr argon, 500 W)



INDUCTIVE DISCHARGES

POWER BALANCE

RESISTANCE AT HIGH AND LOW DENSITIES

• Plasma resistance seen by the coil

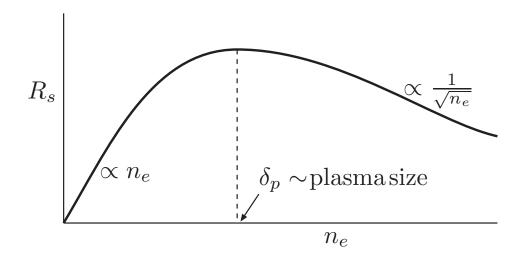
$$R_s = R_p \frac{\omega^2 L_{12}^2}{R_p^2 + \omega^2 L_p^2}$$

• High density (normal inductive operation)

$$R_s \approx R_p \propto \frac{1}{\sigma_{\rm dc}\delta_p} \propto \frac{1}{\sqrt{n_e}}$$

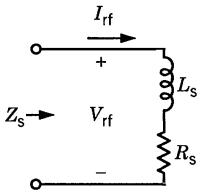
• Low density (skin depth > plasma size)

 $R_s \propto \text{ number of electrons in the heating volume} \propto n_e$

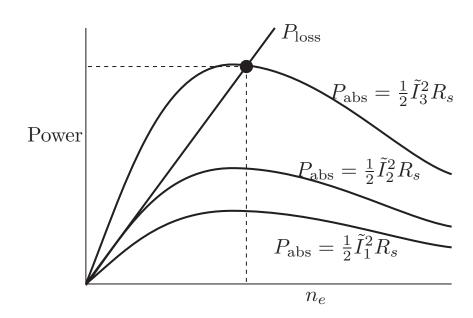


POWER BALANCE WITHOUT MATCHING

• Drive discharge with rf current



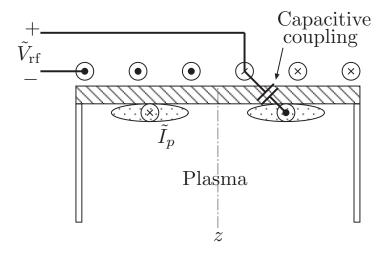
- Power absorbed by discharge is $P_{\rm abs} = \frac{1}{2} |\tilde{I}_{\rm rf}|^2 R_s(n_e)$ Power lost by discharge $P_{\rm loss} \propto n_e$
- Intersection gives operating point; let $\tilde{I}_1 < \tilde{I}_2 < \tilde{I}_3$



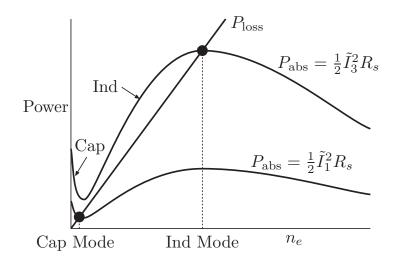
• Inductive operation impossible for $\tilde{I}_{\rm rf} \leq \tilde{I}_2$

CAPACITIVE COUPLING OF COIL TO PLASMA

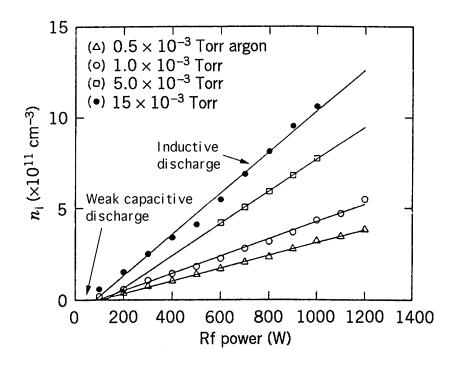
• For \tilde{I}_{rf} below the minimum current \tilde{I}_2 , there is only a weak capacitive coupling of the coil to the plasma



- A small capacitive power is absorbed
 - \Longrightarrow low density capacitive discharge



MEASURMENTS OF ARGON ION DENSITY



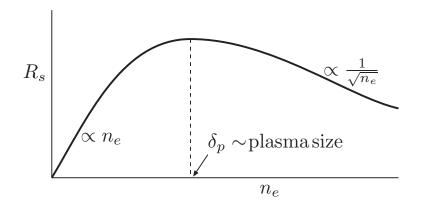
- Above 100 W, discharge is inductive and $n_e \propto P_{\rm abs}$
- Below 100 W, a weak capacitive discharge is present

SOURCE EFFICIENCY

- The source coil has some winding resistance R_{coil}
- R_{coil} is in series with the plasma resistance R_s
- Power transfer efficiency is

$$\eta = \frac{R_s}{R_s + R_{\text{coil}}}$$

• High efficiency \Longrightarrow maximum R_s



- Power transfer efficiency decreases at low and high densities
- Poor power transfer at low or high densities is analogous to poor power transfer in an ordinary transformer with an open or shorted secondary winding

CONCLUSIONS

- Plasma discharges are widely used for materials processing and are indispensible for microelectronics fabrication
- The coupling of the equations for the fields and the charged particles is the key to plasma analysis
- Neutral particles play a key role in ionization, energy loss, and diffusion processes in discharges
- The particle and energy balance relations are the key to the analysis of discharge equilibrium
- The particle balance determines the electron temperature; the energy balance determines the plasma density
- A transformer model along with the particle and energy balance relations are the key to the analysis of inductive discharges